

# Demonstration of Loop Reactor Operation

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*This article is the first experimental demonstration of autothermal operation in an open loop reactor for catalytic abatement of low-concentration volatile organic compounds (VOC). The system under investigation, which comprises three reactors organized in a loop with automatic switching of the feed position, has been successfully operated for ethylene oxidation. The influence of the feed flow rate and concentration on the pulse velocity and maximal temperature has been investigated. A simple analytical approximation for front velocity in the nonadiabatic one-dimensional (1D) model has been derived and compared with the experimental results. © 2008 American Institute of Chemical Engineers AIChE J, 54: 2413–2422, 2008*

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## Introduction

Several conceptual solutions that combine a packed bed and enthalpy recuperation have been suggested for abatement of low-concentration volatile organic compounds (VOC). These include the reverse-flow reactor (RF),<sup>1,2</sup> the loop or ring reactor (LR), which may take several forms as discussed below, the counter-current (CCR)<sup>4</sup> or the internal-recycle reactor and the reactor with external recycle and external heat exchanger. The loop reactor in the form composed of several units with feed switching between them has been simulated by Barresi and coworkers,<sup>3</sup> whereas we have generalized these results by studying the asymptotic solutions of loop reactors, in which a single exothermic reaction occurs.<sup>4</sup> Another form of a circulation loop reactor, in the form of single-port reactor in which a section near the inlet is heated via a heat-exchanger by the exit stream, was suggested by Gilles and Lauschke.<sup>5</sup>

This article is the first experimental verification of VOC combustion in an open loop reactor made of three catalytic reactors. The results are compared to a simple analytical

approximation for front velocity in the nonadiabatic one-dimensional model.

We describe below the main features of reverse-flow and loop reactors. Flow-reversal reactors, in which the feed is varying between two ports, are currently attracting intensive research and have been applied commercially. The advantage of reactors with periodic flow reversal over simple once-through operation for attaining high temperatures has been demonstrated in many studies of adiabatic units during the past decade. This feature makes them especially attractive for VOC oxidation or NO reduction<sup>1,2,6,7</sup> (for a recent review, see Kolios et al.<sup>8</sup>). This high temperature results from the nature of heat loss in the two reactors: in a simple adiabatic fixed bed, the reaction heat is dissipated by convection, whereas in the flow-reversal unit with fast switching, heat is lost mainly by conduction, and this term can be mitigated by building long inert zones on both sides of the catalytic layer. The main advantage of a reactor with flow reversal for combustion purposes is that the bed temperature increases with the flow rate into the reactor, as more material is consumed. Other applications of this technology capitalized on the nonmonotonic temperature profile and were aimed at improving conversion of exothermic reversible equilibrium-limited reactions such as SO<sub>2</sub> oxidation<sup>9,10</sup> and methanol or ammonia synthesis.<sup>11–13</sup>

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**Table 1. Experiments Conditions**

Parameter	Working Area
Velocity (m/s)	0.505–0.732
Residence time (s)	1.64–2.38
Ethylene concentration (% vol)	0.5–0.85
Switching (min)	62.8–533.7
Pressure (atm)	1–1.5

Open Loop reactors extend the two-port concept into feeding at several or many ports in several reactor units that are organized in a loop (Figure 1). To illustrate this concept, a loop reactor with  $N$  units ( $N \geq 2$ ) is considered with a feed port and an exit port that are switched at every predetermined time interval  $\sigma$ . In the first interval, the feed flow enters the first reactor and exits from reactor  $N$ . This pattern will continue as long as the heat front is far from exiting reactor number one. At the second interval, the feed flow enters the second reactor and exits from the first reactor, and so on.

In the desired loop reactor operation, a temperature pulse (hot spot) is formed and rotates around the system. Its temperature can be increased significantly by pushing the pulse; the adiabatic temperature rise across a front in a fixed bed is known to increase with front velocity ( $v_{fr}$ ) (and in turn with the fluid velocity,  $v_o$ ) by a factor of  $(v_o - v_{fr})/(v_o - Le v_{fr})$  compared with the stationary front ( $v_{fr} = 0$ ). Some forms of periodic boundary conditions are required, of course, to sustain the periodic motion. Rotating pulses in a loop reactor may emerge provided that the switching velocity ( $v_{sw}$  i.e., unit length/switching time) and the pulse velocity are matched in a certain way. The maximal temperature in a loop reactor exceeds that in reverse flow reactor.<sup>14</sup>

The main drawback of the loop reactor is the narrow domain of switching velocities that support travelling pulses; the domain becomes narrower with decreasing  $\Delta T_{ad}$  and forms a cusp shaped domain in the  $(\Delta T_{ad}, v_{sw})$  plane.<sup>14</sup> However, the maximal temperature in an adiabatic unit is obtained for  $Le v_{sw}/v_o = 1$ , which should be easy to maintain, if  $Le$  is known. Approximate boundaries of the domain of switching velocities where the pulse solution can be maintained were derived by Nekhamkina and Sheintuch (in press) for a first-order reaction. Because not all parameters (especially  $Le$ ) are known exactly, we incorporate a control mechanism to sustain the pulse.

The article is structured as follows: the experimental apparatus and results are described in following two chapters. The mathematical model is presented in the following chapter along which the approximate solution derived for pulse velocity.

## Experimental

A system made of three fixed bed reactors was arranged in the form of a loop (see Figures 1 and 2 for a flow chart and a schematic chart). We describe below the feed reactor, analysis, and control procedures. There are six control valves, which direct the flow in the system. To assure unidirectional flow in the system, three one-way valves have been con-

structed and placed at the exit of each reactor. These three stainless steel valves were constructed in a way that the flow is directed by a suspended ball, and they can withstand the high temperatures of the system. The other six valves were placed at the cold interface with the tubes outside the vacuum system.

The feed section includes the feed cylinders (ethylene gas, 99.9% purity from Gordon Gas and Chemicals) and compressed air, purification and drying systems, flow controllers, and a rotameter. The compressed air is passed through columns of silica gel and of activated carbon to remove traces of water and hydrocarbons. The system feed (ethylene) is controlled by a mass flow controller (Brooks) that was calibrated and adapted to the system. The air flow is measured by rotameter in a flow range of 10–50 l/min. The outlet  $CO_2$  concentration is measured online by an infrared analyzer with a response time of 20 s (Emproco, Israel).

The three reactors are made of stainless steel (0.029-m diameter and 0.4-m long) and packed by spherical catalytic particles (0.5%, Pt/ $Al_2O_3$  in 2–4-mm diameter, Johnson Matheys, England). The inert section (0.135-m long) was packed by similar size alumina pellet-shaped particles.

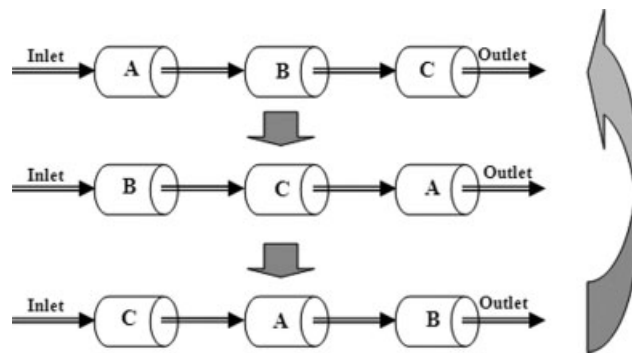
Fifteen thermocouples (type K) were placed along the three reactors and connected to an analog to digital signal convector. The data is displayed and stored in a PC in real time on the computer screen.

For startup purposes, the first reactor is wrapped by a cylindrical heating coil that enabled rapid heating. Following van de Beld (1997)<sup>15</sup> suggestion that the required temperature for full ethylene combustion catalyzed by Pt/ $Al_2O_3$  (0.06%) is 136°C, the initial temperature imposed for the preheated unit in this research was 150°C. When the necessary temperature was achieved, under flow of air, the hydrocarbon was introduced into the system and the heating was turned off.

The three reactors are assembled inside a sealed cylinder (stainless steel 304) connected to a vacuum pump that creates a vacuum (0.7 torr) for the reduction of heat loss; this mechanism was used and studied in many works.<sup>16,17</sup> The inner wall of the cylinder is covered by an aluminum foil to reflect heat radiation from the system.

There are two simple methods for controlling the system:

1. Using constant time intervals predetermined at the beginning of the experiment. This approach is possible

**Figure 1. Scheme of the three-reactor loop system.**

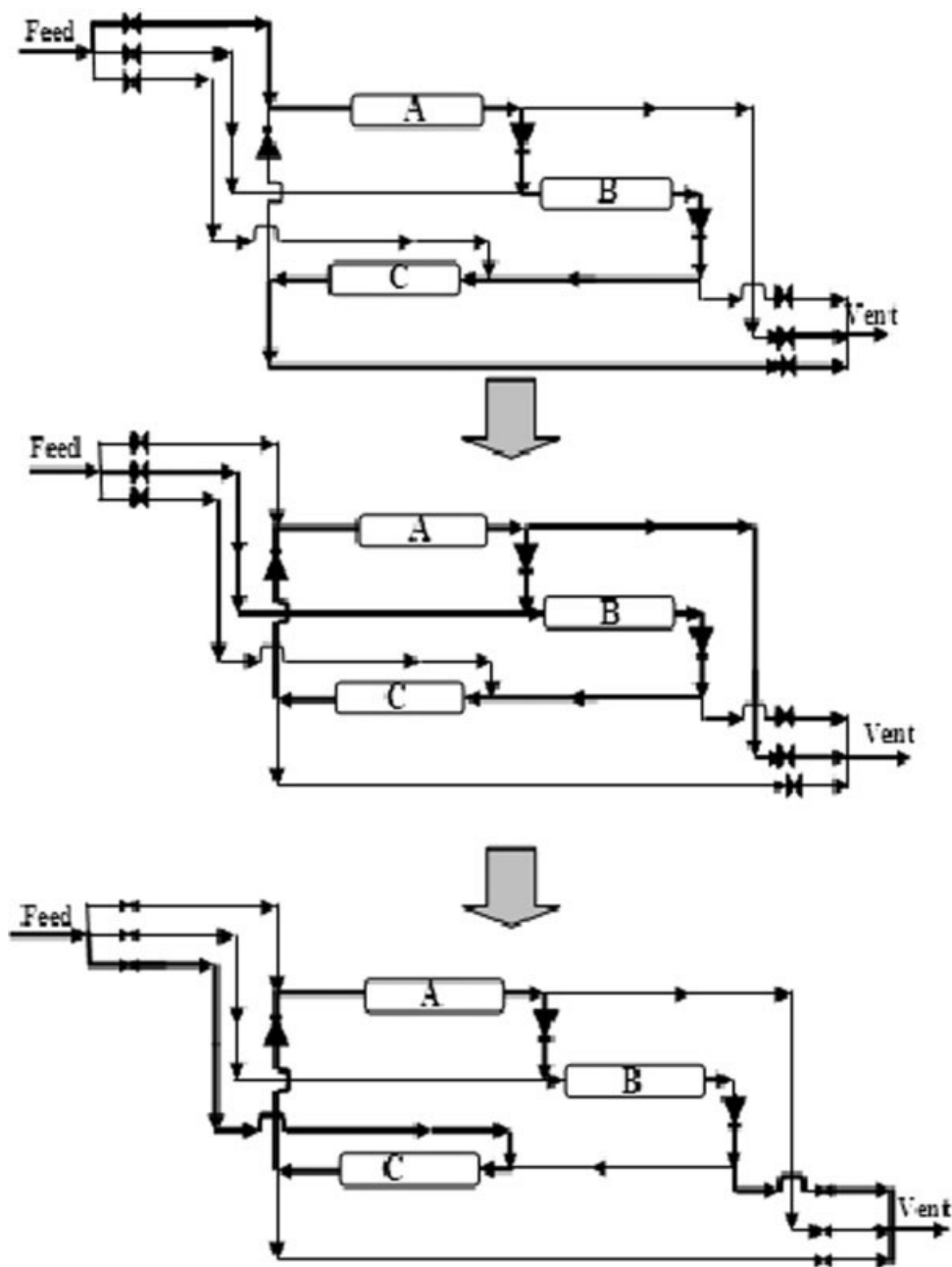


Figure 2. Valve arrangement in the loop reactor system.

when the parameters (especially heat capacity) are known exactly.

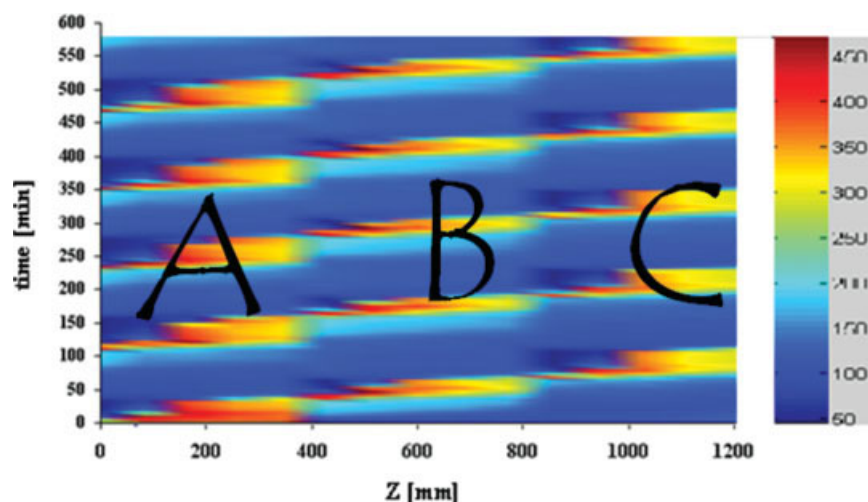
2. Using feedback control to regulate the switching as applied here: for two consecutive reactors, the feed is switched from one reactor to the following when the temperature measured at the entrance of the second reactor reaches  $T_{sw2}$  and the temperature at the entrance of the first reactor drops below  $T_{sw1}$ . This approach was suggested by Barresi and Fissore (2002)<sup>18</sup> and adopted here.

The reaction used in this work, the oxidation of ethylene on  $\text{Pt}/\text{Al}_2\text{O}_3$ , is characterized by high exothermicity and self-inhibition. Its rate was reported to exhibit negative-order kinetics with respect to ethylene at low temperature.<sup>13</sup>

The rate expression reported by Mandler et al. (1983)<sup>19</sup> is

$$r^{\text{Ethylene}} = \frac{k'_{c_1 c_2}}{(1 + K_1 c_1 + K_2 c_2)^2} = \frac{A' \exp(-\frac{E'}{RT}) c_1 c_2}{[1 + A_1 \exp(-\frac{E_1}{RT}) c_1 + A_2 \exp(\frac{E_2}{RT}) c_2]^2} \quad (1)$$

where  $C_1$  and  $C_2$  are ethylene and oxygen concentration in volume percentage. At high temperature, and with oxygen in excess, Eq. 1 is reduced to a simple first-order kinetics.



**Figure 3.** Spatio-temporal color-scaled temperature profile presented in the time-space plane (air flow 25 l/min or 0.63 m/s fluid velocity with 0.7% ethylene in the feed).

[Color figure can be viewed in the online issue, which is available at [www.interscience.wiley.com](http://www.interscience.wiley.com).]

### Experimental results

This is the first demonstration of the loop reactor system for exothermic VOC combustion. We report on the effect of varying feed flow rate and concentration (see Table 1). The switching cycle was determined by the first thermocouple at the entrance of the catalytic area in each reactor as explained above with  $T_{sw1} \cong T_{ign} - 10^\circ\text{C}$  and  $T_{sw2} \cong T_{ign} + 10^\circ\text{C}$ . This control prevents the extinction of the system as well as from temperatures rising to an undesired level that may lead to deactivation.

#### Demonstration of loop-reactor system

A typical spatiotemporal temperature pattern of the system, shown by Figure 3 in a color-scale plot, exhibits a moving pulse pattern. These results were obtained after the reactor was initially heated up in air to  $150^\circ\text{C}$  (i.e., the ignition temperature of ethylene oxidation), and ethylene was subsequently added and the external heating stopped. Figure 4a demonstrated three temperature profiles (three snapshots) inside the closed loop system. Comparison of entire cycles after spatial translation shows overlapping temperature profiles (blue line and light blue line, Figure 4a). The pulse velocity obtained in this case was  $1.75 \times 10^{-4}$  m/s (slope of pattern in Figure 3).

The pulse speed matches the switching speed and depends mainly on the fluid velocity ( $v_o$ ) and on the Lewis number ( $Le$ ), the heat capacity ratio of the bed to the fluid. Theory shows that for an adiabatic system  $v_{sw} \cong v_o/Le$ , yields the highest temperature. Note that  $Le$  is different in unit A due to the heating elements. The temperature profile repeats itself every 114 min ( $L/v_{sw}$ ). In addition, it can be seen that the periodic steady state is attained only after two cycles (Figure 5b).

#### Flow velocity effect

One of the advantages of heat recuperating reactors (RFO, open loop) is that they become more efficient as feed flow

rate increases. Theory shows that increasing the feed flow rate will increase the maximal temperature in an adiabatic unit.<sup>3,4</sup> Another minor effect, which leads to a temperature rise, is due to improvement of mass transfer effects at higher feed velocities. Experiments indeed show that increasing the feed flow rate leads to a linear rise of the maximal temperature in the system (Figure 5a,  $v = 0.5\text{--}0.7$  m/s). Complete conversion was achieved in all cases. It can be also seen that the experimental results are in a good agreement with the analytical approximation we have developed (Eq. 13).

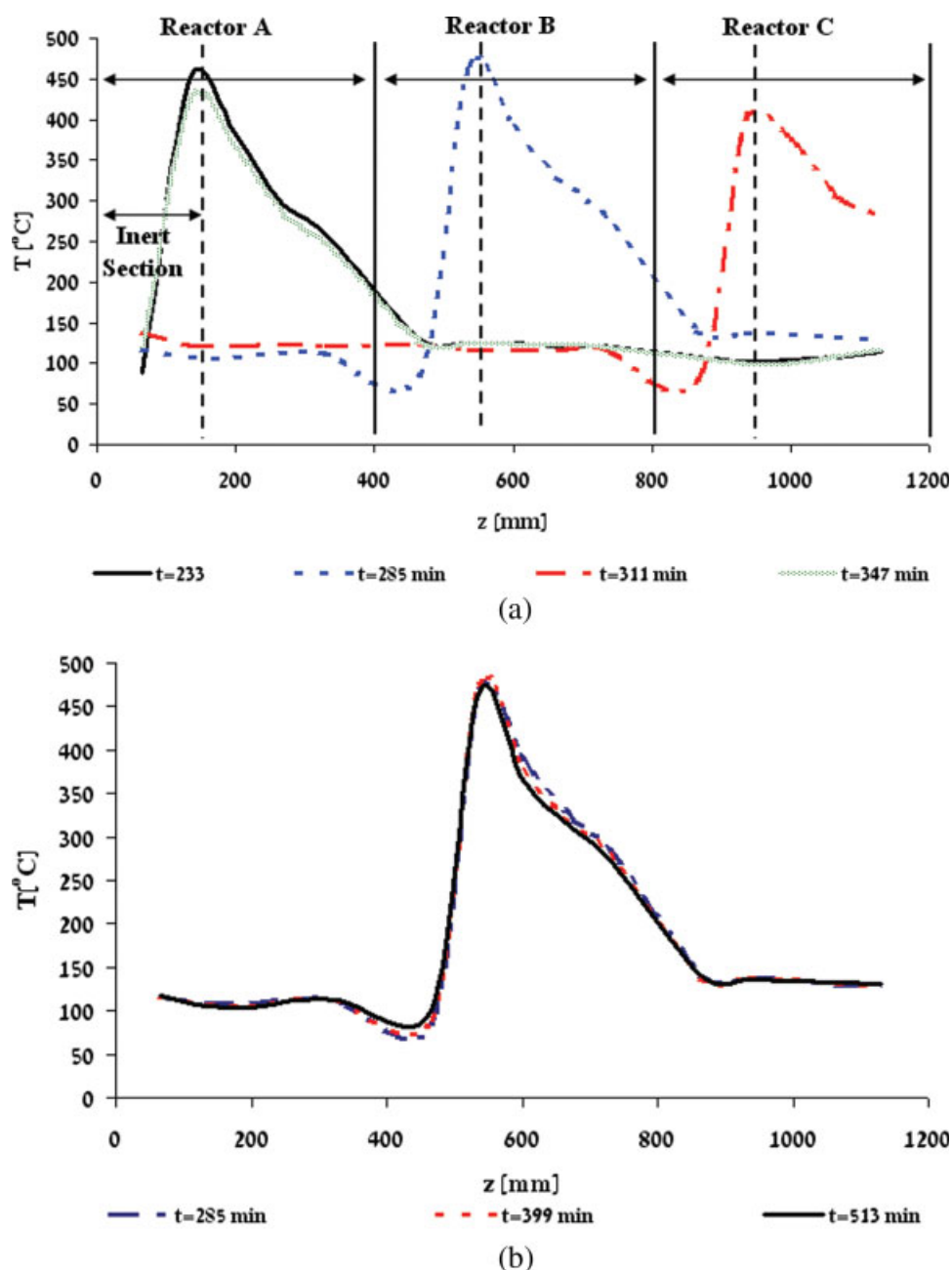
It is expected from the developed approximation that the pulse velocity should increase linearly with the feed velocity (Eqs. 10 and 12). The experimental results obtained within the narrow domain of flow rate studied follows well this prediction (Figure 5b).

#### Effect of contaminant concentration

An additional controllable parameter that can be changed independently is the contaminant (ethylene) concentration, which directly affects the adiabatic temperature rise ( $\Delta T_{ab}$ ). A high concentration of consumed reacted gas ( $C_{in}$ ) is translated to additional energy. Figure 6 shows higher maximal temperatures ( $T_m$ ) obtained in the experiments with increasing  $C_{in}$ . This behavior is also relatively well predicted by the analytical approximation (Figure 6) that also predicts a decline of the pulse velocity with increasing contaminant concentrations.

#### Mathematical model and analytical results

In this section, we derive an expression for the maximal temperature and pulse velocity in a nonadiabatic fixed bed, which are compared with experimental observations (Figures 5 and 6), assuming that the pulse in a loop reactor moves at the switching velocity. Although we are aware of approximate solution for front velocity in a nonadiabatic reactor,<sup>20</sup> we refer



**Figure 4.** Three snapshots of the temperature pulse propagation (a) and their overlapping profiles (b) after spatial translation (conditions in as Figure 3).

[Color figure can be viewed in the online issue, which is available at [www.interscience.wiley.com](http://www.interscience.wiley.com).]

to it at the end of this section and compare our results, showing that it cannot adequately describe our results.

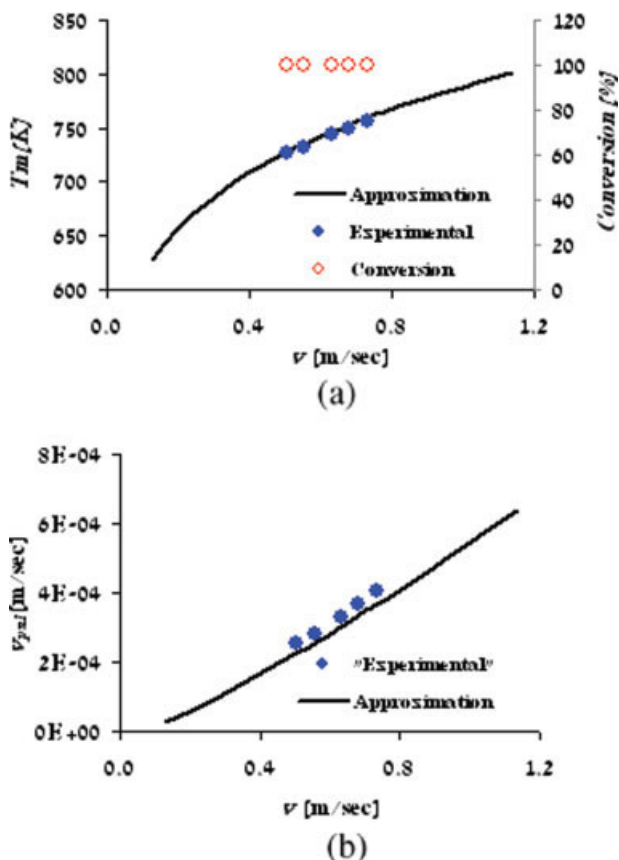
Simulations show that the  $v_{fr}$  in an adiabatic long loop reactor is close to that in a once-through long reactor.<sup>4</sup> We derive the solution for nonadiabatic once-through reactor as an approximation for a bounded nonadiabatic loop reactor.

Consider a pseudohomogeneous one-dimensional (1D) model of a once-through nonadiabatic fixed bed reactor in which a reaction of a general kinetics occurs [ $r(T, C)$  is the rate expression]. The enthalpy and mass balances are described by

$$\begin{aligned}
 (\rho c_p)_s(1 - \varepsilon) \frac{\partial T}{\partial t} + (\rho c_p)_f v_o \frac{\partial T}{\partial z} - k_s \frac{\partial^2 T}{\partial z^2} \\
 = (-\Delta H)(1 - \varepsilon)r(C, T) - \frac{4U}{d}(T - T_w) \quad (2) \\
 \varepsilon \frac{\partial C}{\partial t} + v_o \frac{\partial C}{\partial z} - \varepsilon D \frac{\partial^2 C}{\partial z^2} = -(1 - \varepsilon)r(C, T)
 \end{aligned}$$

With appropriate initial and boundary (Danckwerts) conditions:





**Figure 5.** The dependence of the maximal measured temperature and conversion (a) and the measured pulse velocity (b) on fluid velocity (conditions in as Figure 4).

Also shown is their approximation by the model. [Color figure can be viewed in the online issue, which is available at [www.interscience.wiley.com](http://www.interscience.wiley.com).]

$$\begin{aligned}
 z = z_{in} \quad \varepsilon D \frac{\partial C}{\partial z} &= v_o(C - c_{in}), \quad k_s \frac{\partial T}{\partial z} = (\rho C_p)_f v_o(T - T_{in}) \\
 z = z_{out} \quad \frac{\partial C}{\partial z} &= \frac{\partial T}{\partial z} = 0 \\
 t = 0 \quad C(z) &= C_0; \quad T(z) = T_0
 \end{aligned} \quad (3)$$

We limit our study to generic first-order activated and exothermic reactions with a rate of  $r = A \exp(-E/R_g T)C$ . To a first approximation, the conduction is const ( $k_s$ ), axial dispersion of mass is assumed to be negligible<sup>21</sup> ( $D \rightarrow 0$ ), and thermodynamic parameters ( $\rho$ ,  $C_p$ ) are assumed to be constant. With these assumptions, the system (Eqs. 3 and 4) may be rewritten in the dimensionless form as

$$\begin{aligned}
 \text{Le} \frac{\partial y}{\partial \tau} + \frac{\partial y}{\partial \xi} - \frac{1}{P_{ey}} \frac{\partial^2 y}{\partial \xi^2} &= BDaR - W(y - y_w); \\
 \frac{\partial x}{\partial \tau} + \frac{\partial x}{\partial \xi} &= DaR \\
 R(x, y) &= (1 - x) \exp\left(\frac{\gamma y}{\gamma + y}\right);
 \end{aligned} \quad (4)$$

$$\begin{aligned}
 \tau = 0 : y(0, z) &= y_0, \quad x(0, z) = x_0 \\
 \xi = \xi_{in} \quad \frac{1}{P_{ey}} \frac{\partial y}{\partial \xi} &= y, \quad x = 0 \\
 \xi = \xi_{out} \quad \frac{\partial y}{\partial \xi} &= 0, \quad \frac{\partial x}{\partial \xi} = 0
 \end{aligned} \quad (5)$$

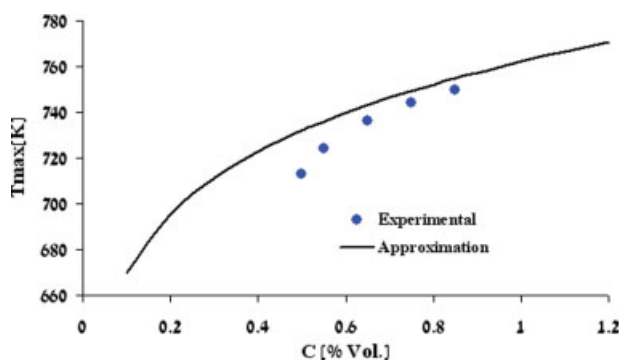
With

$$\begin{aligned}
 x &= 1 - \frac{C}{C_{in}}, \quad y = \gamma \frac{T - T_{in}}{T_{in}}, \quad \xi = \frac{z}{L}, \quad \tau = \frac{tu}{\varepsilon L}, \\
 y &= \frac{E_a}{R_g T_{in}}, \quad B = \gamma \frac{(-\Delta H)C_0}{(\rho C_p)_f T_{in}}, \quad Da = \frac{L(1 - \varepsilon)A}{u} \exp(-\gamma), \\
 \text{Le} &= \frac{(1 - \varepsilon)(\rho C_p)_s}{\varepsilon(\rho C_p)_f}, \quad P_{ey} = \frac{(\rho C_p)_f u L}{k_s}, \\
 W[U, L, d, (\rho C_p)_f, v_o] &= \frac{4UL}{d(\rho C_p)_f v_o}
 \end{aligned}$$

To determine the propagation velocity and the maximal temperature, we assume the thermal front to be ideal, moving along an infinitely long bed at a constant velocity.<sup>21</sup> These conditions are met for an exothermic highly activated irreversible reaction, because a narrow reaction zone is formed (the reaction rate is negligible before and after the front). The corresponding asymptotic solution of the maximal temperature in a slow-switching finite-length loop reactor<sup>14</sup> was shown to approximately follow.

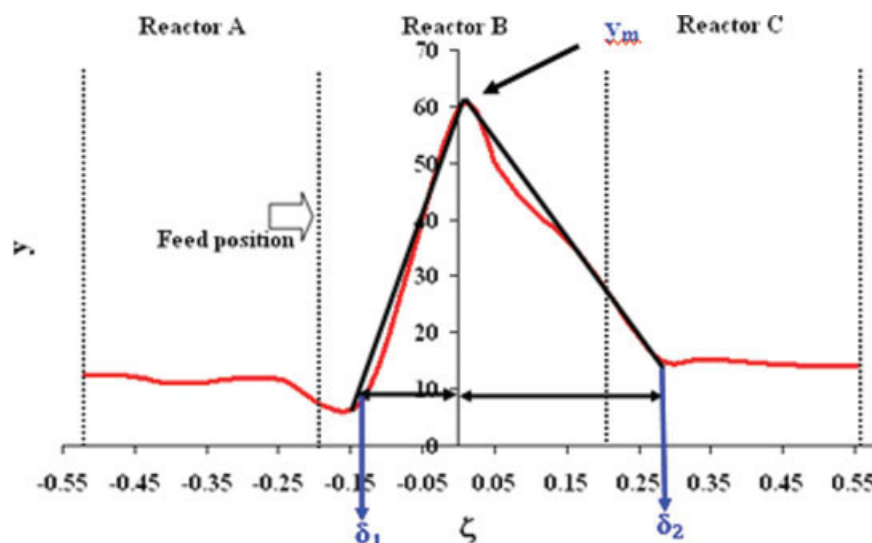
$$F(y_m) = \frac{Da}{P_{ey} B} \left(1 + \frac{y_m}{\gamma}\right)^2 \exp\left(\frac{\gamma y_m}{\gamma + y_m}\right) = \frac{(1 - \varepsilon v_{sw}/v_o)^2}{1 + \alpha(v_{sw}, y_m)} \quad (6)$$

where  $y_m$  is the dimensionless maximal temperature and  $\alpha(v_{sw}, y_m)$  is a correction term due to the finite system length and inhomogeneous boundary conditions;  $\alpha \rightarrow 0$  and  $v_{sw} \rightarrow v_\infty$  for an unbounded reactor. The solution of front movement in an unbounded once-through system is quite similar, with<sup>22</sup>  $F(y_m) \rightarrow (1 - \varepsilon v_{fr}/v_o)^2$ . This similarity between the



**Figure 6.** The dependence the measured and approximated maximal temperature on feed concentration (fluid velocity is 0.63 m/s).

[Color figure can be viewed in the online issue, which is available at [www.interscience.wiley.com](http://www.interscience.wiley.com).]



**Figure 7. An actual pulse and its triangle-shaped approximation used in the derivation.**

[Color figure can be viewed in the online issue, which is available at [www.interscience.wiley.com](http://www.interscience.wiley.com).]

switching velocity ( $v_{sw}$ ), defined as  $v_{sw} = \Delta L/\sigma$ , in a long loop reactor and the front velocity ( $v_{fr}$ ) in an unbounded once-through reactor is expected to hold here as well in the nonadiabatic case. In such a case, it is convenient to transform the governing Eq. 4 using a moving coordinate system with fixed positions of the inlet and outlet:

$$t = t', \quad z' = z - v_{sw}t$$

And, in dimensionless coordinates

$$\tau = \tau', \quad \zeta = \zeta - \omega\tau, \quad \omega = \frac{\varepsilon v_{sw}}{v_o}$$

$$\begin{aligned} L_e \frac{\partial y}{\partial \tau'} + (1 - L_e \omega) \frac{\partial y}{\partial \zeta} &= \frac{1}{P_{ey}} \frac{\partial^2 y}{\partial \zeta^2} + BD_a R - W(y - y_w) \\ \frac{\partial x}{\partial \tau'} + (1 - \omega) \frac{\partial x}{\partial \zeta} &= D_a R(x, y) \end{aligned} \quad (7)$$

We try to derive such an approximation based on a “steady” frozen front solution ( $\partial y/\partial \tau' = \partial x/\partial \tau' = 0$ ).

In a similarity to an “ideal” front in an adiabatic system, we can define an “ideal” front in a nonadiabatic with the exit temperature  $y$  ( $\zeta \rightarrow \infty$ ) =  $y_w$ . For an “ideal” front in an infinitely long system, the boundary condition are modified to

$$\begin{aligned} \zeta \rightarrow -\infty, \quad y &\equiv 0 \quad \frac{\partial y}{\partial \zeta} \equiv 0, \quad x \rightarrow 0 \\ \zeta \rightarrow +\infty \quad y &\equiv y_w \equiv 0 \quad \frac{\partial y}{\partial \zeta} \equiv 0 \end{aligned}$$

The mass and heat balances in stationary Eq. 7 can be added as follows:

$$\begin{aligned} (1 - \omega L_e) \frac{\partial y}{\partial \zeta} &= \frac{1}{P_{ey}} \frac{\partial^2 y}{\partial \zeta^2} + B(1 - \omega) \frac{\partial x}{\partial \zeta} - W y \\ (1 - \omega) \frac{\partial x}{\partial \zeta} &= D_a R(x, y) \end{aligned} \quad (8)$$

In an adiabatic ( $W = 0$ ) “ideal” front, a simple integration of Eq. 8 allows to obtain a relation between the maximal temperature rise and the front velocity:

$$(1 - \omega L_e) y_m = B(1 - \omega) x_m.$$

In the nonadiabatic case, the temperature profile is assumed, for simplicity, to be linear at the pulse front ( $-\delta_1 < \zeta < 0$ ) and at its back ( $0 < \zeta < \delta_2$ ) (Figure 7). To estimate the effect of the heat losses, we integrate the heat loss in a triangularlike spatial temperature profile (Figure 7) and integrate Eq. 8 (from  $-\infty$  up to 0) to find

$$\begin{aligned} -\infty < \zeta < 0 &\Rightarrow 0 = (1 - L_e \omega) y_m - B(1 - \omega) x_m + \frac{W y_m \delta_1}{2} \\ 0 < \zeta < \infty &\Rightarrow 0 = -(1 - L_e \omega) y_m + \frac{W y_m \delta_2}{2} \end{aligned} \quad (9)$$

and with  $\delta_1$  to be determined later from experimental results. Equation 9 for  $\zeta < 0$  can be written as

$$y_m = \frac{B(1 - \omega) x_m}{(1 + \frac{W \delta_1}{2} - L_e \omega)} \quad (10)$$

An inspection of Eq. 7 shows that  $\omega < 1$  (otherwise  $\partial x/\partial \zeta < 0$ ). To ensure that  $y_m > 0$ , the dimensionless heat front velocity must obey  $L_e \omega < (1 + W \delta_1/2)$ .

Equation 10 provides relation between  $\omega$  and  $y_m$ ;  $\omega$  cannot be determined, as the value of  $y_m$  is unknown. To calculate  $\omega$ , let us integrate Eqs. 8 under certain simplifying assumption.

$$\begin{aligned} \frac{\partial y}{\partial \zeta} &= P_{ey} \frac{(1 - \omega) B}{y_m} y - y P_{ey} \frac{W \delta_1}{2} \\ &\quad - P_{ey} \frac{y_m W \delta_1}{2} - P_{ey} B(1 - \omega) x + P_{ey} W \int_{\zeta}^0 y d\zeta \end{aligned} \quad (11)$$

We shall use the extrapolation method developed by Kiselev (1993). As is shown in the Appendix, the main impact of various

terms can be estimated by their values around the front position. To simplify the problem, we can replace the last term of Eq. 11 by its approximation,  $P_{ey}W_{ym}\delta_1$ .

In Appendix, we show (Eqs. A7) that the pulse velocity is

$$\omega = 1 - \frac{(\gamma + y_m)}{\gamma} \sqrt{\frac{D_a K(y_m)}{P_{ey} B}} \quad K(y_m) = \exp\left(\frac{\gamma y_m}{\gamma + y_m}\right) \quad (12)$$

Substituting  $\omega$  from Eq. 10 into Eq. 12, we obtain an equation with respect to a single unknown variable  $y_m$ :

$$\frac{D_a}{P_{ey} B} \left(1 + \frac{y_m}{\gamma}\right)^2 \exp\left(\frac{\gamma y_m}{\gamma + y_m}\right) = \frac{y_m^2 (1 + \frac{W\delta_1}{2} - Le)^2}{(B - y_m Le)^2} \quad (13)$$

In adiabatic system ( $W \rightarrow 0$ ), we obtain

$$\frac{D_a}{P_{ey} B} \left(1 + \frac{y_m}{\gamma}\right)^2 \exp\left(\frac{\gamma y_m}{\gamma + y_m}\right) = \frac{y_m^2 (1 - Le)^2}{(B - y_m Le)^2} \quad (14)$$

which for  $Le \gg 1$  and  $y_m Le \gg B$  is reduced to

$$F(y_m) = \frac{D_a}{P_{ey} B} \left(1 + \frac{y_m}{\gamma}\right)^2 \exp\left(\frac{\gamma y_m}{\gamma + y_m}\right) = 1 \quad (15)$$

which agrees with solutions in the literature (Eq. 6)

Gattica et al.<sup>20</sup> developed an approximation for maximal temperature and front velocity using similar assumptions as well as assuming that the reaction zone is extremely narrow:

$$y_m = \frac{B(1 - \omega)}{\left((1 - Le \omega)^2 + \frac{4W}{Pe_y}\right)^{1/2}} \quad (16)$$

$$\omega = 1 - \left(\frac{y_m + \gamma}{\gamma}\right) \sqrt{\frac{D_a K(y_m)}{P_{ey} B}}$$

When comparing our approximation, which uses an experimentally determined value of pulse width ( $\delta_1$ ) with theirs, we find that  $\delta_1$  should be

$$\delta_1 = W(Le \omega - 1) \left[1 - \sqrt{1 + \frac{4W}{Pe_y(1 - Le \omega)^2}}\right] \quad (17)$$

Using the experimental values, we find  $\delta_1 \sim 10^{-3}$  vs.  $\delta_1 \sim 10^{-1}$  determined from Figure 7; therefore, in this work, an alternative approximation was developed.

### Application

We use Eq. 13, using the experimentally determined value of  $\delta_1$  (Figure 7) to predict the maximal temperature and the pulse velocity.

As the discussion at the end of the previous chapter shows, the procedure describes well the experimental observations in Figures 5 and 6.

### Conclusions

A system of loop-shaped reactor network was experimentally investigated as an alternative to the reverse-flow reactor.

The system including three reactors, each with an inert section, with feedback control of feed position has been successfully operated for ethylene oxidation. The system can be controlled by a simple set of two switches activated by crossing two temperature set points. This strategy serves for startup and is stable with respect to fluctuating inlet concentrations and also of gas flow rates. Increasing feed flow rate and feed ethylene concentration were found to lead to higher front velocities and reactor maximal temperatures. An analytical approximation for the heat front velocity and the maximal reactor temperature in a nonadiabatic system has been developed. The experimental results are in a good agreement with the derived analytical approximations.

The loop reactor may admit higher temperatures than those of the RF reactor, and, when deactivation cannot be avoided, it spreads evenly around the system. Yet, the loop reactor requires more valves and a feedback control. This work shows that the latter obstacles can be overcome.

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### Notation

#### Symbols

$A$  = pre-exponential factor ( $s^{-1}$ )  
 $B$  = dimensionless temperature rise in adiabatic model  
 $C$  = concentration ( $gmol\ m^{-3}$ )  
 $C_{pF}$  = gas heat capacity ( $kJ\ kg^{-1}\ K^{-1}$ )  
 $C_{pS}$  = solid heat capacity ( $kJ\ kg^{-1}\ K^{-1}$ )  
 $d$  = reactor diameter (m)  
 $D$  = effective axial mass dispersion ( $m^2\ s^{-1}$ )  
 $Da$  = Damkohler number  
 $E_a$  = activation energy ( $kJ\ gmol^{-1}$ )  
 $k_s$  = solid thermal conductivity ( $kJ\ m^{-1}\ s^{-1}\ K^{-1}$ )  
 $K$  = another dimensionless reaction ( $m^3\ gmol^{-1}$ )  
 $L$  = reactor length (m)  
 $Le$  = Lewis number in adiabatic model  
 $Pe_y$  = Peclet number for heat in adiabatic model  
 $r$  = reaction rate ( $gmol\ s^{-1}$ )  
 $R$  = dimensionless reaction rate  
 $R_g$  = gas constant ( $8.314\ kJ\ kmol^{-1}\ K^{-1}$ )  
 $t$  = time (s)  
 $t'$  = time in a moving coordinate (s)  
 $T$  = temperature (K)  
 $T_{in}$  = inlet temperature (K)  
 $T_{ign}$  = ignition temperature (K)  
 $T_m$  = maximal temperature (K)  
 $T_{sw}$  = switch temperature (K)  
 $T_w$  = wall temperature (K)  
 $U$  = heat transfer coefficient ( $kJ\ m^{-2}\ s^{-1}\ K^{-1}$ )  
 $W$  = dimensionless heat transfer coefficient  
 $v_o$  = gas velocity  
 $v_{fr}$  = heat front velocity (s)  
 $v_{sw}$  = switch velocity (s)  
 $w$  = another dimensionless temperature  
 $x$  = conversion  
 $x_m$  = maximal conversion  
 $y$  = dimensionless temperature  
 $y_m$  = dimensionless maximal temperature  
 $y_w$  = dimensionless wall temperature



$z$  = axial coordinate (m)  
 $z'$  = axial coordinate in a moving coordinate (m)  
 $-\Delta H$  = heat of combustion ( $\text{kJ gmol}^{-1}$ )

## Greek letters

$\gamma$  = dimensionless activation energy  
 $\Delta T_{\text{ad}}$  = adiabatic temperature rise (K)  
 $\varepsilon$  = reactor bed void fraction  
 $\sigma$  = switching period (s)  
 $\zeta$  = dimensionless axial coordinate  
 $\rho_g$  = gas density ( $\text{kg m}^{-3}$ )  
 $\rho_s$  = solid density ( $\text{kg m}^{-3}$ )  
 $\tau$  = dimensionless time  
 $\tau'$  = dimensionless time in a moving coordinate  
 $\omega$  = dimensionless front velocity  
 $\zeta$  = dimensionless axial coordinate in a moving coordinate

## Abbreviations

CCR = counter-current reactor  
 LR = loop reactor or ring reactor  
 RF = reverse flow  
 VOC = volatile organic compounds

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## Appendix

We follow the procedure of Kiselev<sup>22</sup> to determine the maximal temperature: introducing a new variable  $w = y/y_m$ , Eq. 12 in text can be rewritten as

$$\frac{\partial w}{\partial \zeta} = \frac{P_{cy}B}{y_m}(1-\omega) \left[ (w-x) - w \frac{y_m W \delta_1}{2B(1-\omega)} \right] \quad (A1)$$

$$(1-\omega) \frac{\partial x}{\partial \zeta} = D_a R$$

$$\frac{y_m W \delta_1}{2B(1-\omega)} = Q, \quad K(y_m) = \exp\left(\frac{\gamma y_m}{\gamma + y_m}\right)$$

Dividing the two equations mentioned earlier, we obtain

$$\frac{\partial x}{\partial w} = \frac{y_m D_a K(1-x)}{P_{cy}B(1-\omega)^2[w(1-Q)-x]} \quad (A2)$$

Assuming full conversions ( $x_m = 1$ ) at the pulse (peak), we obtain

$$\frac{\partial x}{\partial w} = f(w, x) = p(w)g(w, x), \quad (A3)$$

$$p(w) = \frac{y_m D_a K}{P_{cy}B(1-\omega)^2}, \quad g(w, x) = \frac{(1-x)}{w(1-Q)-x}$$

Note that  $g(w, x)$  possesses a singularity if  $x \rightarrow 1$  while  $w \rightarrow 1$  and  $0 < Q \ll 1$ ; however, the limits  $g(w, x)$  and  $dx/dw$  ( $x'_w$ ) are finite

$$\lim_{w, x \rightarrow 1} x'_w = \lim_{w, x \rightarrow 1} f(w, x) = p(1) \frac{-x'_w}{1-x'_w} \quad (A4)$$

$$\lim_{w, x \rightarrow 1} x'_w = 1 + P(1)$$

Integrating Eq. A2, we obtain

$$1 = \int_0^1 p(w)g(w, x)dw \quad (A5)$$

Using the assumption of a narrow reaction zone, the integral in (A5) can be approximated as

$$x(w) = 1 - x'_w(1 - w)$$

and substitute in (A3)

$$g(w, x) \cong \frac{x'_w(1 - w)}{w - 1 + x'_w(1 - w)}$$

Using now (A4)

$$g(w, x) \cong \frac{1 + P(1)}{1 + P(1) - 1} = 1 + \frac{1}{P(1)} \cong 1$$

Here, we assume that  $P(1) \gg 1$ .<sup>22</sup> Substituting  $g(w, x)$  into Eq. A5, we obtain  $\int_0^1 p(w)dw = 1$  or

$$\frac{y_m D_a}{P_{ey} B(1 - \omega)^2} \int_0^1 \exp\left[\frac{\gamma(w y_m)}{\gamma + w y_m}\right] dw = 1 \quad (\text{A6})$$

Equation 11 for a closed system with respect to the two unknown ( $\omega$  and  $y_m$ ). The integral in Eq. A5 can be esti-

mated using the Frank-Kamenetski<sup>21</sup> approach. Consider the power in the area of  $w = 1$ :

$$\begin{aligned} \frac{\gamma(w y_m)}{\gamma + w y_m} \Big|_{w \rightarrow 1} &\cong \frac{\gamma y_m}{\gamma + y_m} + \frac{\gamma y_m(\gamma + w y_m) - \gamma y_m^2}{(\gamma + y_m)^2} \Big|_{w=1} (w - 1) \\ &\quad + o((w - 1)^2) \\ \frac{\gamma(w y_m)}{\gamma + w y_m} \Big|_{w \rightarrow 1} &= \frac{\gamma y_m}{\gamma + y_m} + \frac{\gamma^2 y_m(w - 1)}{(\gamma + y_m)^2} \end{aligned}$$

Now the integral in the LHS of Eq. A5 is

$$\begin{aligned} \int_0^1 p(w)dw &\cong \frac{y_m D_a}{P_{ey} B(1 - \omega)^2} \exp\left[\frac{\gamma y_m}{\gamma + y_m}\right] \int_0^1 \exp\left[\frac{\gamma^2 y_m(w - 1)}{(\gamma + y_m)^2}\right] dw \\ &= \frac{D_a(\gamma + y_m)^2 K(y_m)}{\gamma^2 P_{ey} B(1 - \omega)^2} \left[1 - \exp\left[\frac{-\gamma^2 y_m}{(\gamma + y_m)^2}\right]\right] \cong \frac{D_a(\gamma + y_m)^2 K(y_m)}{\gamma^2 P_{ey} B(1 - \omega)^2} \end{aligned}$$

As the last term in the square brackets can be neglected in comparison with one. Equation 25 can be reduced to the following algebraic equation:

$$\frac{D_a(\gamma + y_m)^2 K(y_m)}{\gamma^2 P_{ey} B(1 - \omega)^2} = 1 \quad K(y_m) = \exp\left(\frac{\gamma y_m}{\gamma + y_m}\right) \quad (\text{A7})$$

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